

Loudspeaker Parameters

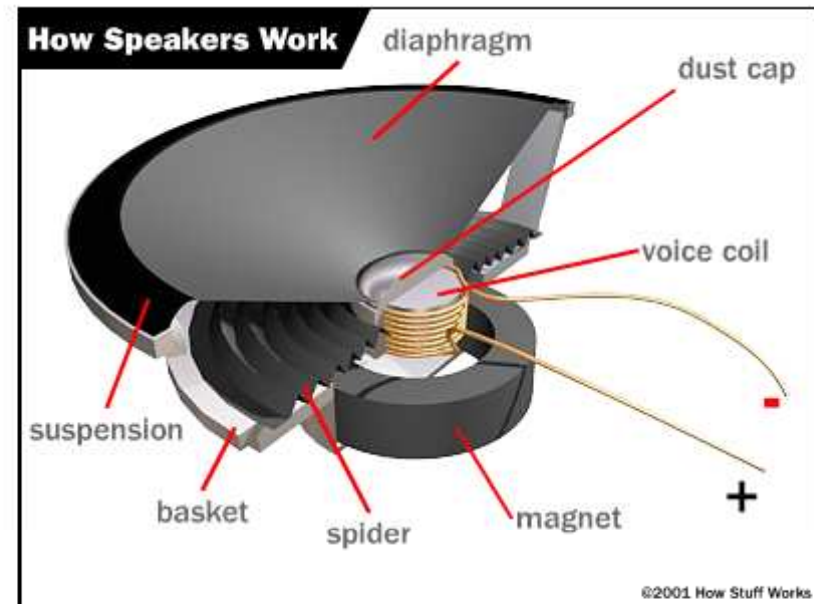
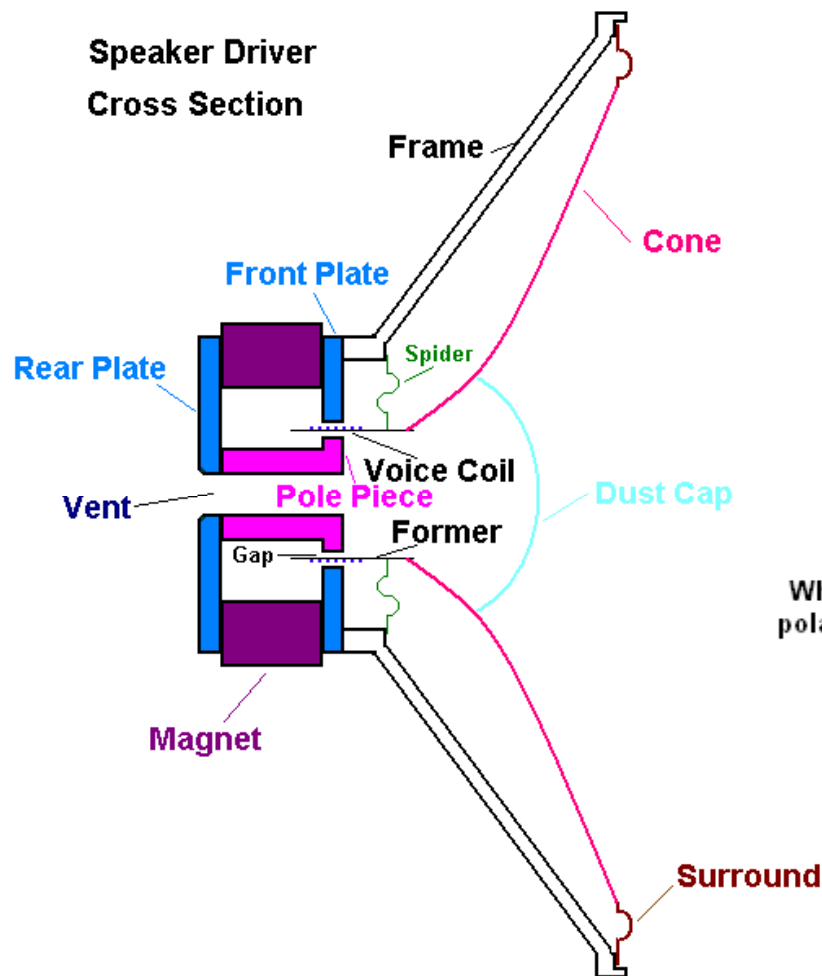
D. G. Meyer

School of Electrical & Computer
Engineering

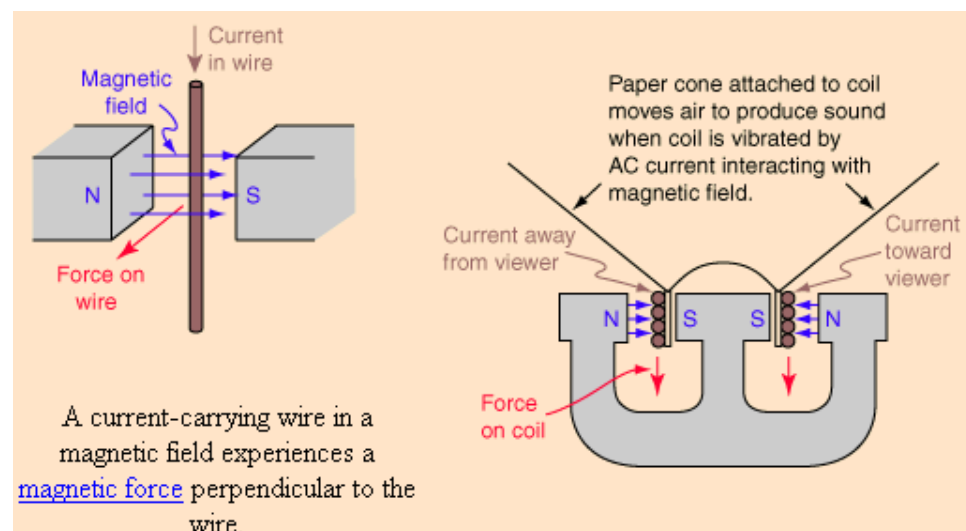
Outline

- **Review of How Loudspeakers Work**
- **Small Signal Loudspeaker Parameters**
- **Effect of Loudspeaker Cable**
- **Sample Loudspeaker**
- **Electrical Power Needed**
- **Sealed Box Design Example**

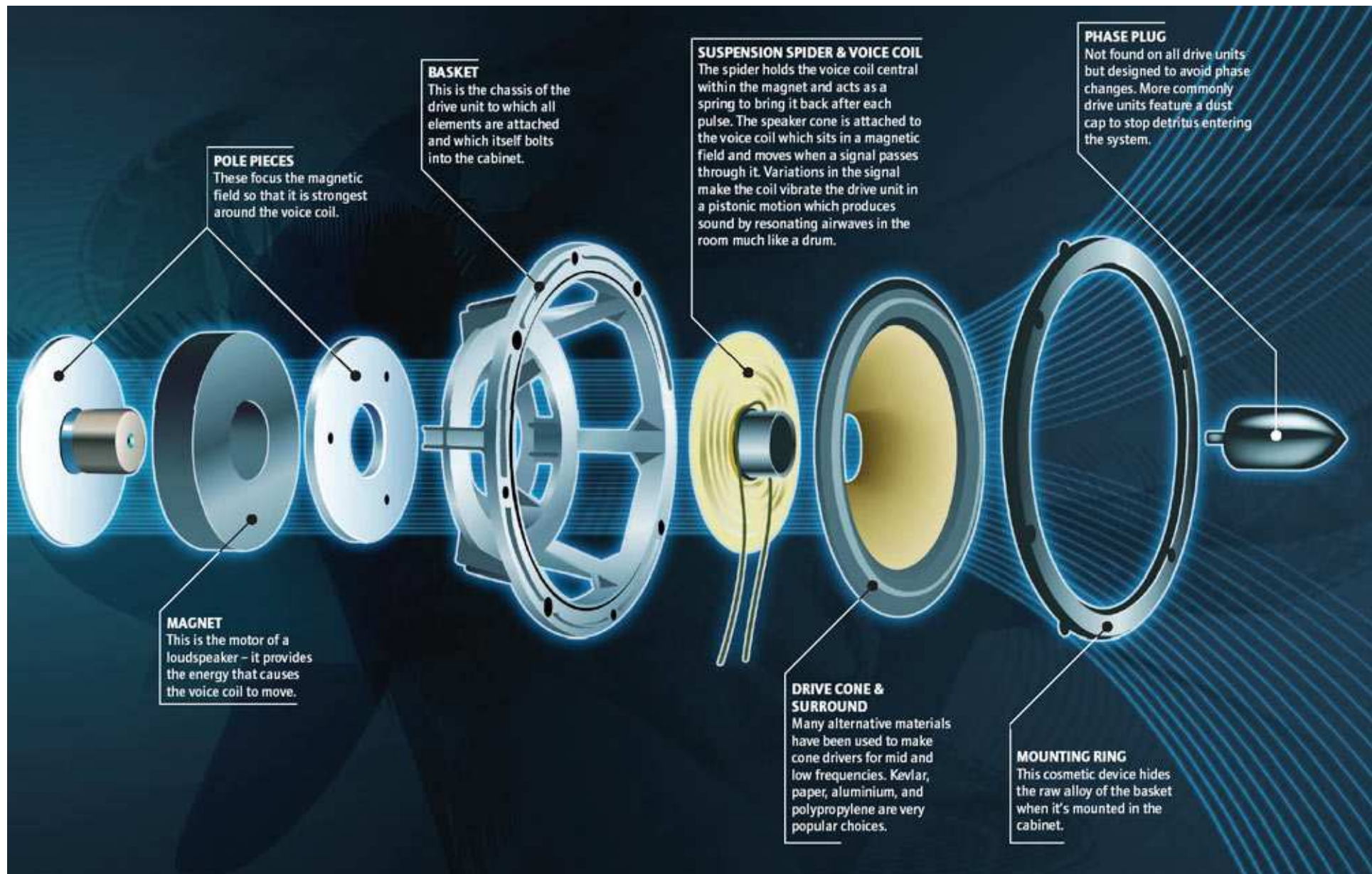
How Loudspeakers Work



When the electrical current flowing through the voice coil changes direction, the coil's polar orientation reverses. This changes the magnetic forces between the voice coil and the permanent magnet, moving the coil and attached diaphragm back and forth.



How Loudspeakers Are Made



Fundamental Small Signal Mechanical Parameters

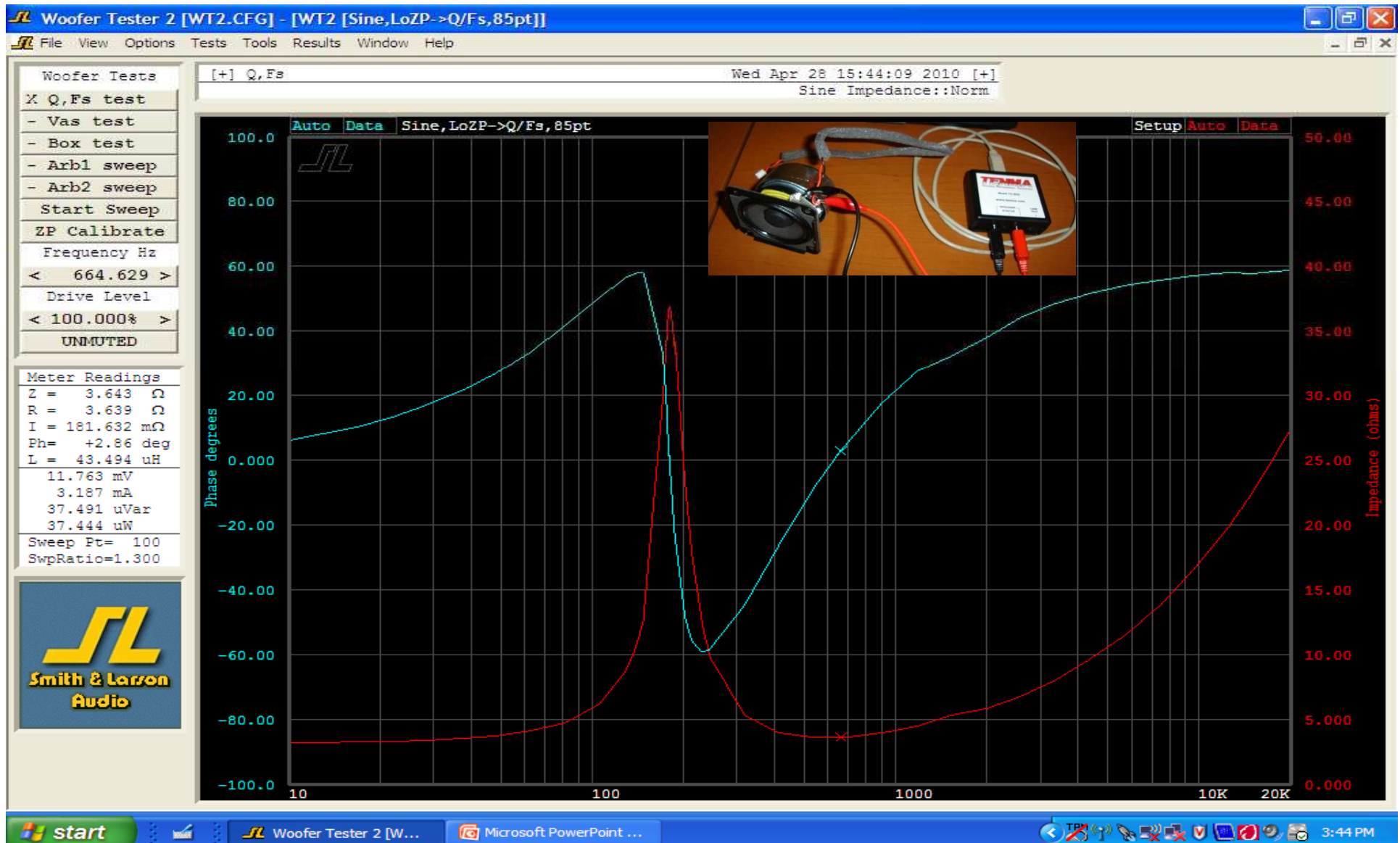
- S_d – projected area of driver diaphragm (m^2)
- M_{ms} – mass of diaphragm (kg)
- C_{ms} – compliance of driver's suspension (m/N)
- R_{ms} – mechanical resistance of driver's suspension ($\text{N}\cdot\text{s}/\text{m}$)
- L_e – voice coil inductance (mH)
- R_e – DC resistance of voice coil (Ω)
- Bl – product of magnetic field strength in voice coil gap and length of wire in magnetic field ($\text{T}\cdot\text{m}$)

Small Signal Parameters

These values can be determined by measuring the input impedance of the driver, near the resonance frequency, at small input levels for which the mechanical behavior of the driver is effectively linear.

- **F_s – (free air) resonance frequency of driver (Hz)**
 - frequency at which the combination of the energy stored in the moving mass and suspension compliance is maximum, which results in maximum cone velocity
 - usually it is less efficient to produce output frequencies below F_s
 - input signals significantly below F_s can result in large excursions
 - typical factory tolerance for F_s spec is $\pm 15\%$

Measurement of Loudspeaker Free-Air Resonance



Small Signal Parameters

These values can be determined by measuring the input impedance of the driver, near the resonance frequency, at small input levels for which the mechanical behavior of the driver is effectively linear.

- **Q_{ts} – total Q of driver at F_s**
 - unitless measurement, characterizing the combined electrical and mechanical damping of the driver
 - proportional to the energy stored, divided by the energy dissipated
 - most drivers have Q_{ts} values between 0.2 and 0.5

Small Signal Parameters

These values can be determined by measuring the input impedance of the driver, near the resonance frequency, at small input levels for which the mechanical behavior of the driver is effectively linear.

- **Q_{ms} – mechanical Q of driver at F_s**
 - unitless measurement, characterizing the mechanical damping of the driver, i.e., losses in the suspension (surround and spider)
 - varies roughly between 0.5 and 10 (typical value is 3)
 - high Q_{ms} indicates lower mechanical losses
 - main effect of Q_{ms} is on impedance: high Q_{ms} drivers display a higher impedance peak

Small Signal Parameters

These values can be determined by measuring the input impedance of the driver, near the resonance frequency, at small input levels for which the mechanical behavior of the driver is effectively linear.

- **Q_{es} – electrical Q of driver at F_s**
 - a unitless measurement, describing the electrical damping of the speaker
 - as the coil of wire moves through the magnetic field, it generates a current which opposes the motion of the coil (“back EMF”)
 - the back EMF decreases the total current through the coil near F_s , reducing cone movement and increasing impedance
 - Q_{es} is the dominant factor in voice coil damping for most drivers (depends on amplifier output impedance)

Aside: How Does Loudspeaker Cable And Power Amplifier Output Impedance Affect Performance?

- Damping is a measure of a power amplifier's ability to control the back EMF motion of the loudspeaker cone after the signal disappears
- The **damping factor** of a system is the ratio of the loudspeaker's nominal impedance to the total impedance driving it
- Example: Amplifier with damping factor of 300 (bigger is better) driving an 8Ω load means that the output impedance is 0.027Ω (lower is better)
- Impedance of speaker cable used can significantly reduce the damping factor (larger gauge wire has lower impedance)

Line Loss Calculator - Microsoft Internet Explorer


File Edit View Favorites Tools Help

Back

Search

Favorites

Address http://www.crownaudio.com/apps_htm/designtools/line-loss.htm Go Links

 **crown**

INTELLIGENT POWER. UNLEASHED.

Products Applications Support Press Corporate Extra Secure Area

Line Loss

[\[Back to Design Tools\]](#)

Power Driven on Line <input type="text" value="100"/> watts	Length of Line <input type="text" value="200"/> ft.
Voltage level <input type="text" value="15"/> volts	Wire Gauge <input type="text" value="#18 AWG"/>
<input type="button" value="Reset"/>	Line Loss:
<input type="button" value="Calculate"/>	<input type="text" value="-3.3"/> dB

This calculator provides line loss with 2-conductor cable on a constant voltage line.

Equation used to calculate the data:

$$P_{loss} = 10 * \text{Log} [1 - ((2 * RL) / (2 * RL + (V_{line} \text{ squared} / Prated)))]$$

Done

Wednesday, October 03, 2007

Small Signal Parameters

These values can be determined by measuring the input impedance of the driver, near the resonance frequency, at small input levels for which the mechanical behavior of the driver is effectively linear.

- **V_{as} – equivalent compliance volume (volume of air which, when acted upon by a piston of area S_d , has the same compliance as the driver's suspension)**
 - measure of the “stiffness” of the suspension with the driver mounted in free air
 - represents the volume of air that has the same stiffness as the driver's suspension when acted upon by a piston of the same area (S_d) as the cone
 - larger values mean lower stiffness (and generally require larger enclosures)
 - V_{as} varies with the square of the speaker's diameter
 - typical factory tolerance for V_{as} is $\pm 20\text{-}30\%$

Sample Loudspeaker

4" Aluminum Cone Woofer

MCM Audio Select Part #: 55-1856 | MCM Order #: 55-1856

[All Categories](#) [Audio & Video](#)



No reviews yet!

[Write a review](#)

Versatile driver offers high power capacity and wide frequency response making it ideal in applications including full range and midbass in compact monitors. Large vented magnet, heavy duty voice coil and thick aluminum cone provide tremendous durability in high SPL applications.



Sensitivity = 86 dB

$F_s = 65 \text{ Hz}$

$R_e = 6.6 \Omega$

$L_e = 0.48 \text{ mH}$

$Q_{ts} = 0.365$

$Q_{es} = 0.436$

$Q_{ms} = 2.25$

$V_{as} = 3.15 \text{ liters}$

Product Description

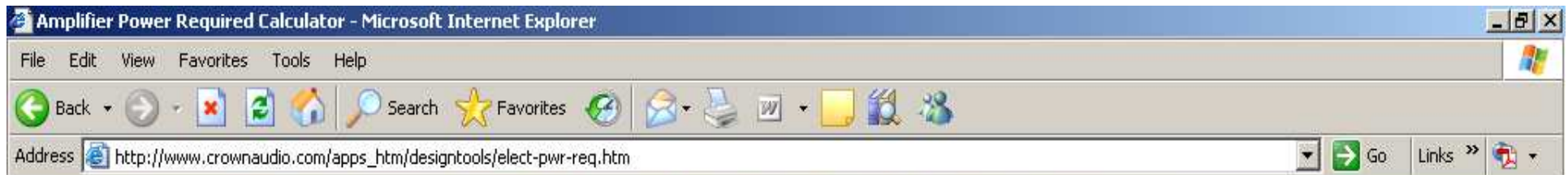
- Aluminum cone
- Synthetic dust cap
- Rubber surround
- Stamped steel basket
- 1" copper voice coil
- 17.7oz magnet

Specifications:

- Power Capacity: 50W/100W RMS/peak
- Sensitivity: 86dB (W/M)
- Impedance: 8Ω
- R_e : 6.6Ω
- L_e : 0.48mH
- Frequency response: 65Hz ~ 17KHz
- F_s : 65Hz
- Q_{ts} : 0.365
- Q_{es} : 0.436
- Q_{ms} : 2.25
- V_{as} : 3.15 (liters)
- X_{max} : 2.25mm
- Overall frame diameter: 4.13" (pincushion)
- Required cutout: 3.66"
- Mounting depth: 2.5"

Aside: How Loud Does This Thing Get? (And, How Much Power Do I Need?)

- Relating electrical power needed to produce desired SPL at a given listening distance:
 - sensitivity rating of loudspeaker (typically spec as 1 m on-axis with input of 1 electrical watt)
 - acoustic level change/attenuation between loudspeaker and farthest listening position
- Example: want 90 dB program level at listening distance of 4 m outdoors (i.e., no reinforcement of sound due to room reflections)
 - loudspeaker sensitivity measured as 86 dB
 - acoustic level change = $20 \log (4) \cong 12 \text{ dB}$
 - SPL required at source is $90 + 12 = 102 \text{ dB}$
 - need 16 dB above 1 watt, or $10^{(16/10)} = 40 \text{ W}$
 - **check to make sure driver can handle it!**



Amplifier Power Required

<http://www.crownaudio.com>

[\[Back to Design Tools\]](#)

Listener Distance from source 32 M	Desired Level at Listener distance 90 dBSPL
Loudspeaker Sensitivity Rating (1W/1M) 110 dB	Amplifier Headroom 10 dB
Calculate	Required Amplifier Power 102 watts
Reset	

Equations used to calculate the data:

$$dBW = L_{req} - L_{sens} + 20 * \log (D2/D_{ref}) + HR$$

$$W = 10 \text{ to the power of } (dBW / 10)$$

Where:

L_{req} = required SPL at listener

L_{sens} = loudspeaker sensitivity (1W/1M)

$D2$ = loudspeaker-to-listener distance

D_{ref} = reference distance

HR = desired amplifier headroom

dBW = ratio of power referenced to 1 watt

W = power required

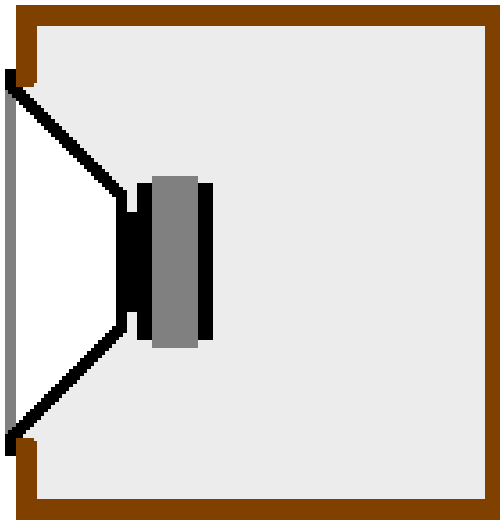
This calculator provides the required electrical power (power output from the amplifier) to produce a desired Sound Pressure Level (SPL) at a given distance, along with an amount of headroom to keep the amplifier(s) out of clip.

Example: You are designing a system where the farthest listening position from the loudspeaker is 100 meters, and the desired Sound Pressure Level is 85 dB SPL. The loudspeaker chosen for the job has a sensitivity rating of 95 dB. With the minimum recommended amplifier headroom of 3 dB, then you need to choose an amplifier that can supply at least 1,995 watts to the loudspeaker.

Enclosure-Related Parameters

- **$EBP = F_s / Q_{es}$**
 - used loosely to decide what type of enclosure will be best for a given speaker (“rule of thumb”)
 - sealed box $EBP \approx 50$
 - vented enclosure $EBP \approx 100$
- **F_c = sealed enclosure resonance**
- **V_c = internal volume of a sealed enclosure**
- **V_b = internal volume of a vented enclosure**
- **F_b = bass reflex enclosure resonance**
- **L_v = length of port**
- **Q_{tc} – desired value determines size and type of enclosure**
 - value of 0.707 is what most designers aim for (yields flattest response)
 - enclosures designed to enhance bass may range from 0.8 to 1.1 (bigger value, “boomier” sound)
 - enclosures that are too big ($Q_{tc} < 0.707$) can sound “tinny”

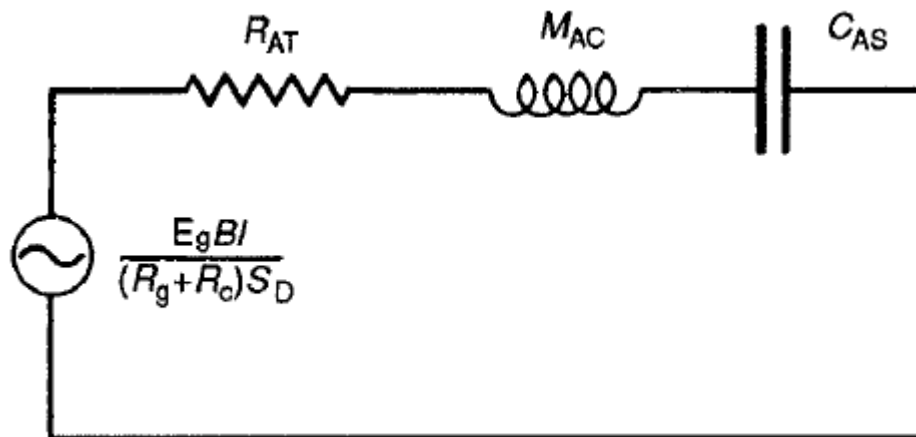
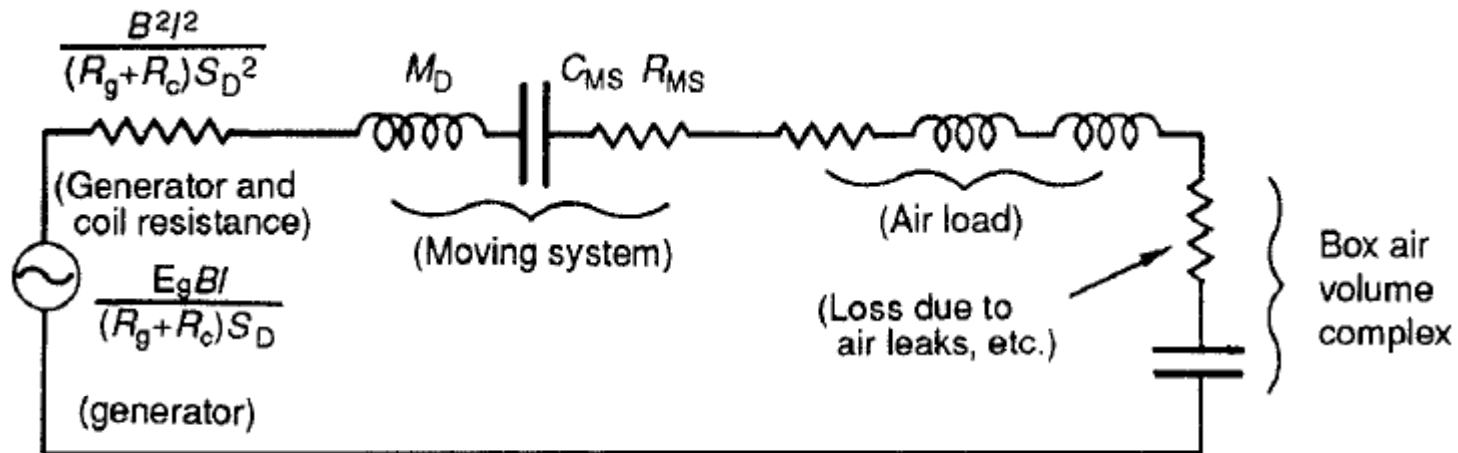
Sealed Box



Sealed Box

- Theoretically an infinite baffle with an additional stiffness component added (to the existing suspension compliance) due to the springiness of the air volume trapped in the enclosure
- A smaller box will have a greater stiffness contribution than a larger one – in sealed box systems the air restoring force is normally made dominant (compared with that of the driver suspension)

Electromechanical Equivalent for Driver in a Sealed Box

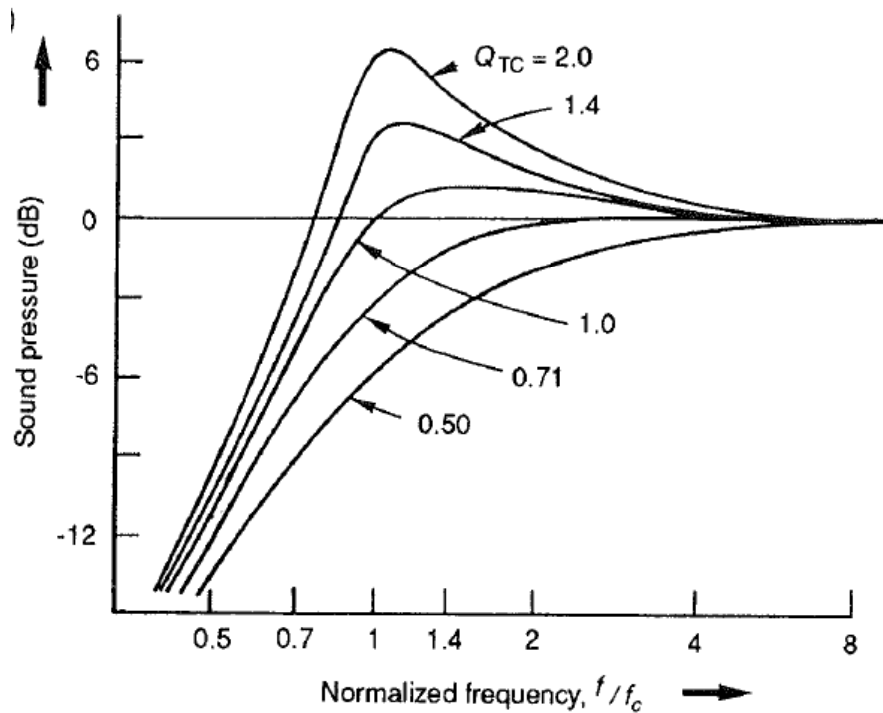


Simplified form –
system response is
that of a damped
single-resonant circuit

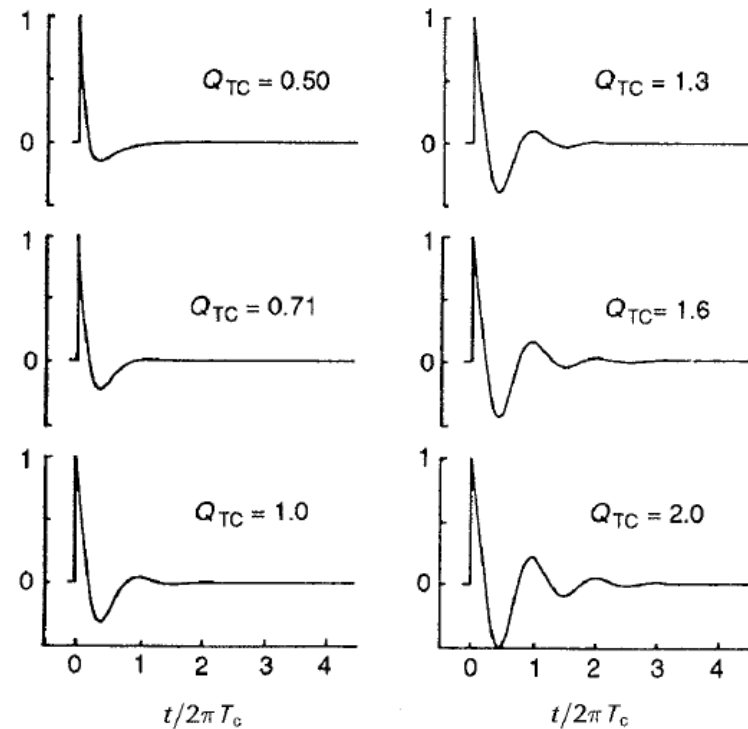
Response Shape

- Critically damped ($Q_{TC} = 0.5$): response is -6 dB at resonance (no ringing/overshoot in transient response)
- Butterworth alignment ($Q_{TC} = 0.7$): response is -3 dB at resonance (response is “maximally flat” and has good transient behavior)
- $Q_{TC} = 1$: provides greater bandwidth at expense of transient response accuracy
- Chebychev alignment ($Q_{TC} = 1.1$): 2 dB peak in response at resonance – results in optimum efficiency alignment for a sealed box system, and is permissible for a small system of limited bandwidth (e.g., F_C of 65 Hz and above)

Behavior of a Closed-Box Loudspeaker System for Several Values of Total System Q_{TC}



Amplitude vs. Normalized Frequency Response



Normalized Step Response

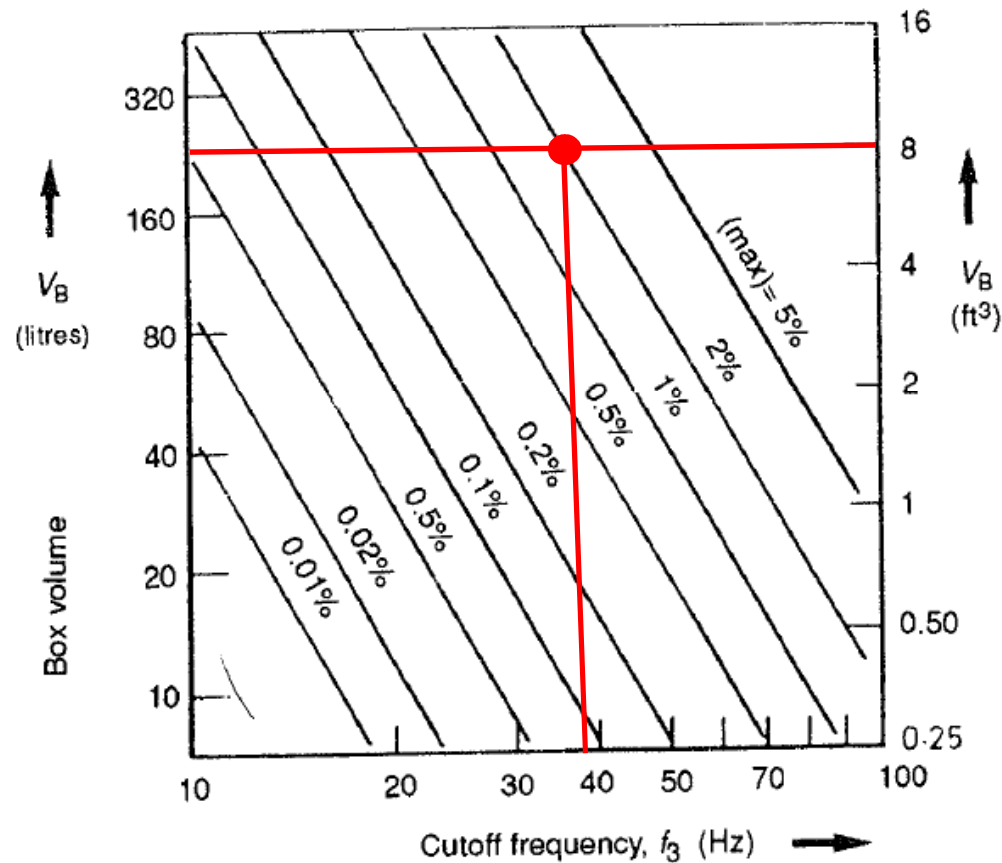
Enclosure Volume and Efficiency

- The maximum efficiency even a large sealed-box enclosure can achieve is small (1-2%)
- Increasing the box cutoff frequency increases the theoretical efficiency
- The closed-box system efficiency in the passband region (system reference efficiency) is the reference efficiency of the driver operating with the particular value of air-load mass provided by the system enclosure
- Reference efficiency (η_0) calculation:

$$\eta_0 = 4\pi^2/c^3 \times (F_S^3 V_{AS})/Q_{ES} = 4\pi^2/c^3 \times (F_C^3 V_{AT})/Q_{EC}$$

where V_{AT} is a volume of air having the same total acoustic compliance as the driver suspension and enclosure acting together

Relationship of Maximum Reference Efficiency to Cutoff Frequency and Enclosure Volume



Example: An 8 cu. ft. (e.g. 2'x2'x2') sealed box with a reference efficiency (η_0) of 2% would have a cutoff frequency (F_c) of slightly less than 40 Hz

Chart for Chebychev Alignment

Box Filling or Damping

- Stuffing may offer an apparent air volume increase of up to 15%
- Additionally, stuffing may add a mass component due to physical movement of the filling at lower frequencies
- Combined effects lower the system resonance and must be accounted for in the design (the effective cone mass increase could be as much as 20%)
- Very dense fillings will increase frictional air losses in the enclosed air volume and augment the damping
- If system is designed correctly, such damping is not required, but may help control a system where the Q_{TC} is too high (e.g., due to inadequate magnet strength)
- Movement of the filling is undesirable!

Sealed Box Design

- Compliance Ratio: $\alpha = V_{AS} / V_B$

- System-driver relationships:

$$Q_{TC}/Q_{TS} \approx Q_{EC}/Q_{ES} = F_C/F_S = (\alpha + 1)^{0.5}$$

$F_C / Q_{TC} \approx F_S / Q_{TS}$ where Q_{TS} is the total Q of the driver at F_S for zero source resistance, i.e.

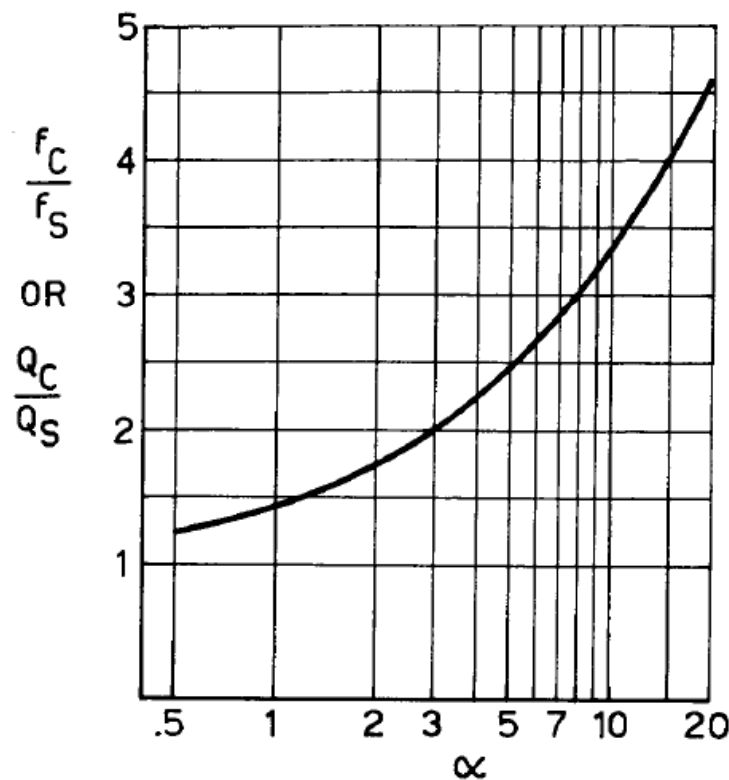
$$Q_{TS} = Q_{ES} Q_{MS} / (Q_{ES} + Q_{MS})$$

- These equations show that for any enclosure-driver combination the speaker resonance frequency must always be lower than that of the system resonance frequency (i.e., value of α) and Q will be in the same ratio as those of the driver, but individually raised by a factor of $(\alpha+1)^{0.5}$
- Provides guidance for both “fixed driver” designs and designs where only a final system specification is given

Ratio of Closed-Box System Resonance Frequency (F_C) and Total Q (Q_{TC})
to Driver Resonance Frequency (F_S) and Q_T ,
as a Function of the System Compliance Ratio (α)

f_C = box cutoff
frequency

f_S = loudspeaker
free-air resonance
frequency



Compliance Ratio: $\alpha = V_{AS} / V_B$

Sealed Box Design Example

- $F_s = 31 \text{ Hz}$
- $Q_{ES} = 0.77$
- $Q_{MS} = 1.89$
- $V_{AS} = 65.8 \text{ liters}$
- $\eta_0 = 4\pi^2/c^3 \times (F_s^3 V_{AS})/Q_{ES}$
 $= (9.64 \times 10^{-7}) \times (31^3 \times 65.8)/0.77 = 2.45\%$
- effective diaphragm radius = 10.2 cm (0.102 m),
giving $S_D = 3.27 \times 10^{-2} \text{ m}^2$
- peak linear displacement (Xmax) given as 3.8 mm
 $(3.8 \times 10^{-3} \text{ m})$
- peak displacement volume = $V_D = S_D X_{\text{max}} = 1.24 \times 10^{-4} \text{ m}^3$
 (124 cm^3)
- power rating given as 70W RMS

$EBP = 40 \rightarrow \text{use sealed enclosure}$



Sealed Box Design Example

- constraints
 - driver resonance frequency (F_S) must always be lower than that of the system (F_C)
 - α must be at least 3
 - Q_{TS} must be lower than highest acceptable Q_{TC}
 - V_{AS} must be at least several times larger than the enclosure size (volume)
 - select most desirable combination of F_C and Q_{TC} that satisfies $F_C / Q_{TC} \approx F_S / Q_{TS}$ and then calculate $\alpha = V_{AS} / V_B$
- calculations
 - $Q_{TS} = (0.77)(1.89)/(0.77+1.89) = 0.547$
 - based on $\alpha \geq 3$ requirement, $F_C/F_S \geq 2 \rightarrow F_C \geq 62$
 - $F_S / Q_{TS} = 56.7 \approx F_C / Q_{TC} \rightarrow$ for $F_C = 62$ get $Q_{TC} \approx 1.1$ (“Chebychev Alignment” \rightarrow maximum efficiency)
 - internal volume of box needed based on α
 $\alpha = V_{AS} / V_B$ (want $\alpha \geq 3$) $\rightarrow V_B \leq 22$ liters (0.022 m^3)
 - yields approximate size of: $0.28 \text{ m} \times 0.28 \text{ m} \times 0.28 \text{ m}$



Speaker Parameters

Qtc: Vas: liters
 Qts: Pmax: watts
 Qes: Diameter: cm
 Fs: Hz Xmax: mm

Calculate

www.ajdesigner.com

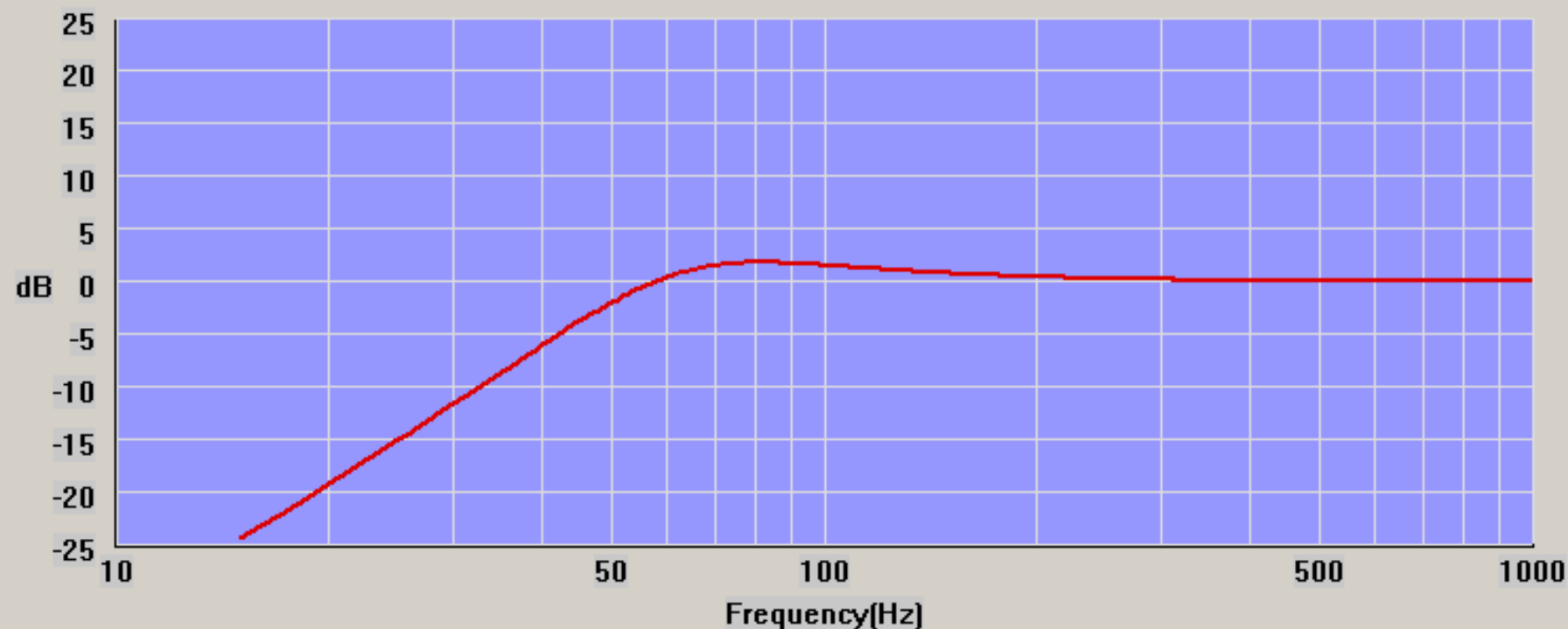
☒ Output Response

☐ Power Response

Box Results

Vb: liters
 Fb: Hz
 F3: Hz

Frequency Response: Output vs. Frequency



Box Calculator



Vb (liter):

Addl. V (liter):

Total V (liter):

Length (cm):

☐

Constrain

Width (cm):

☐

Constrain

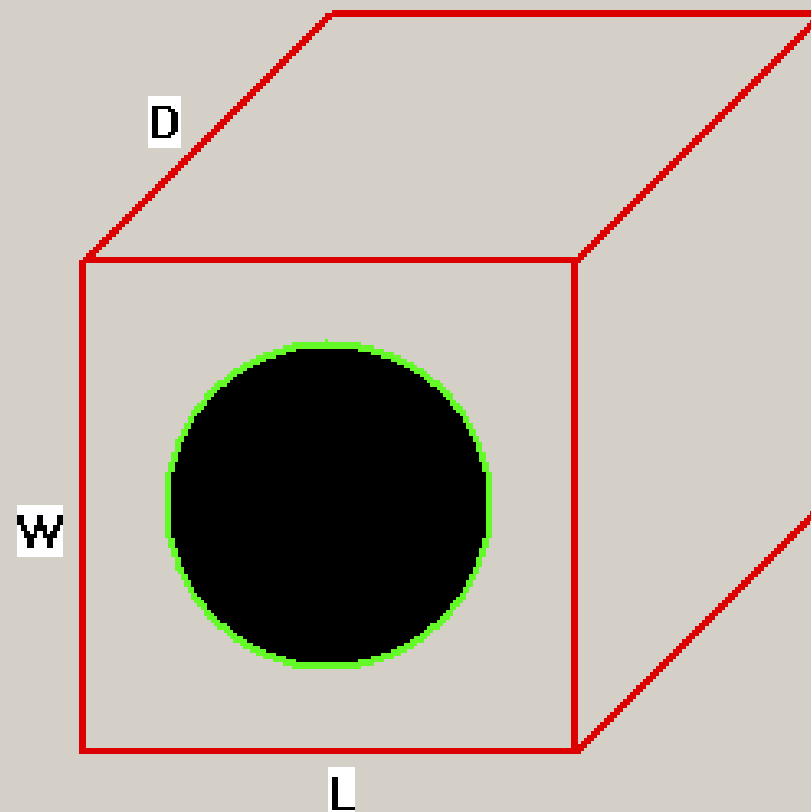
Depth (cm):

☐

Constrain

Calculate

Cancel



Speaker Parameters

Qtc: 0.7 Vas: 65.8 liters
 Qts: 0.55 Pmax: 70 watts
 Qes: 0.77 Diameter: 20.32 cm
 Fs: 31 Hz Xmax: 3.8 mm

Calculate

www.ajdesigner.com

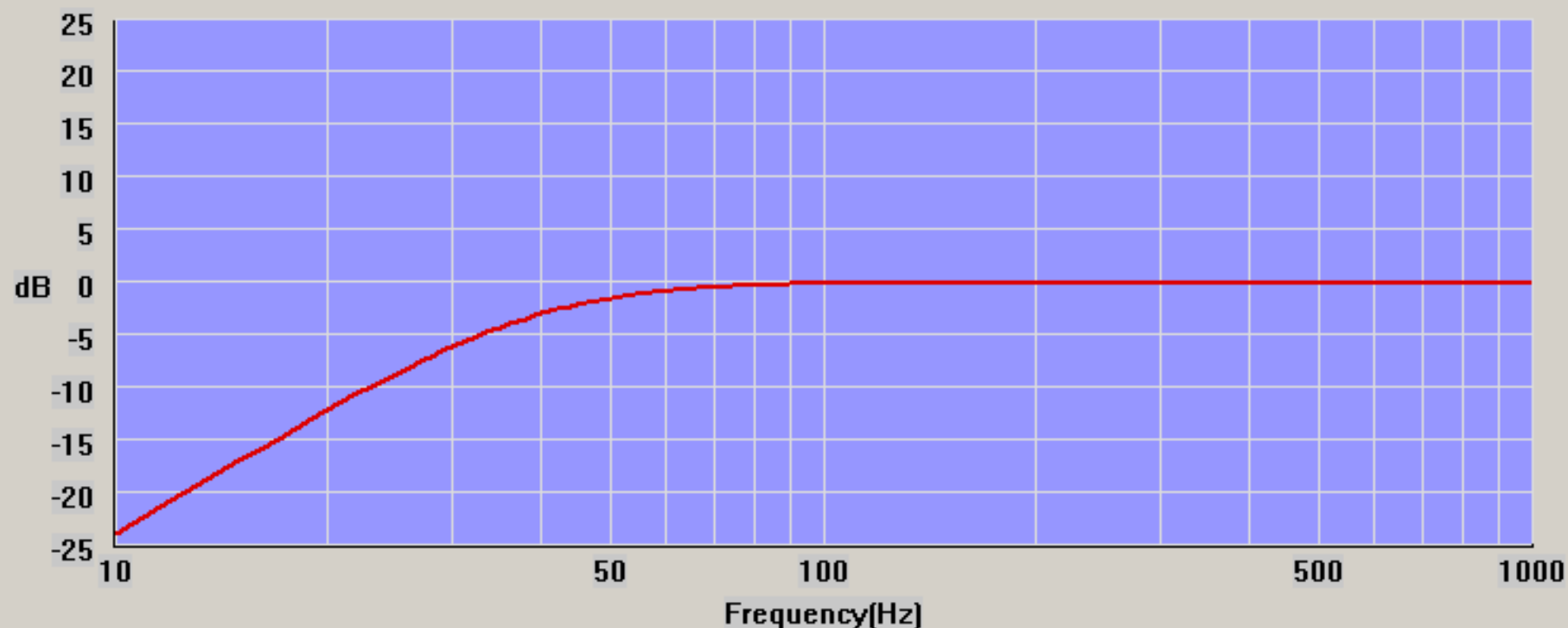
☒ Output Response

☐ Power Response

Box Results

Vb: 106.157 liters
 Fb: 39.4545 Hz
 F3: 39.8592 Hz

Frequency Response: Output vs. Frequency





Vented Box Design Example

- alignments (choice depends on Q_{ts})
 - QB3 – quasi 3rd order Butterworth
 - SBB4 – 4th order Butterworth (“maximally flat”)
 - C4 – 4th order Chebychev
- need to determine port size/length


10" Woofer with Poly Cone and Rubber Surround 100W
MCM Part #: 55-2972 | MCM Audio Select Part #: 55-2972

[All Categories »](#) [Audio & Video](#)

★★★★★ 5 stars from 2 reviews.
[Login to rate or review this product](#)



- Ideal in two or three way applications, or as a subwoofer
- Suitable for sealed or vented enclosures
- 100W/200W RMS/peak
- Polypropylene cone
- Rubber surround
- 1.5" voice coil
- 24oz. magnet

 Product Description

- Sensitivity: 90dB (W/M)
- Impedance: 8ohm
- Re: 7.2ohm
- Le: 0.56mH
- Frequency response: 50Hz-5KHz
- Fs: 40Hz
- Qts: 0.45
- Qes: 0.55
- Qms: 2.49
- Vas: 82.27 liters
- Xmax: 5mm
- Overall frame diameter: 10.00"
- Required cutout: 9.01"
- Mounting depth: 4.29"

Speaker Parameters

Qts: Diameter: cm
 Qes: Xmax: mm Alignment: ☒ SBB4
 Fs: Hz Dp: cm ☐ QB3
 Vas: liters # Ports: ☐ SC4
 Pmax: watts

Calculate

www.ajdesigner.com

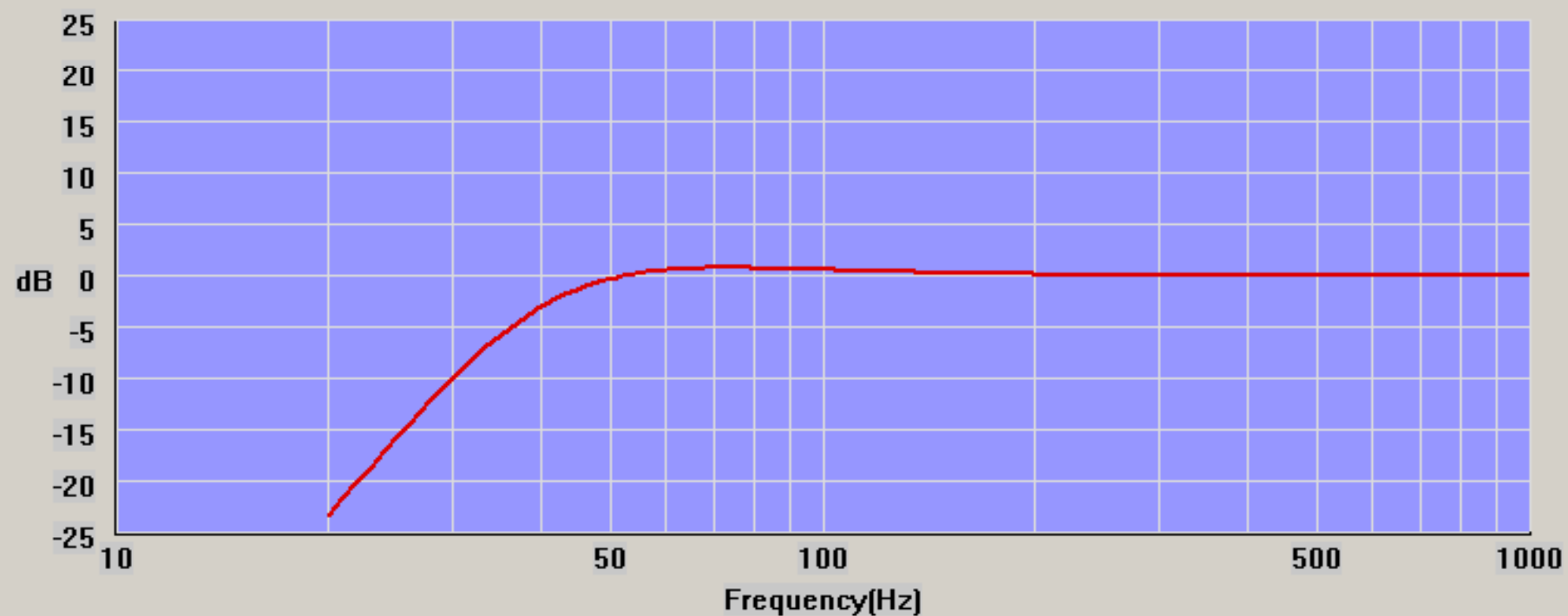
☒ Output Response

☐ Power Response

Box Results

Vb: liters
 Fb: Hz
 F3: Hz
 Lp: cm

Frequency Response: Output vs. Frequency



Speaker Parameters

Qts: Diameter: cm

Qes: Xmax: mm

Fs: Hz Dp: cm

Vas: liters # Ports:

Pmax: watts

Alignment:

☐ SBB4

☒ QB3

☐ SC4

Calculate

www.ajdesigner.com

☒ Output Response

☐ Power Response

Box Results

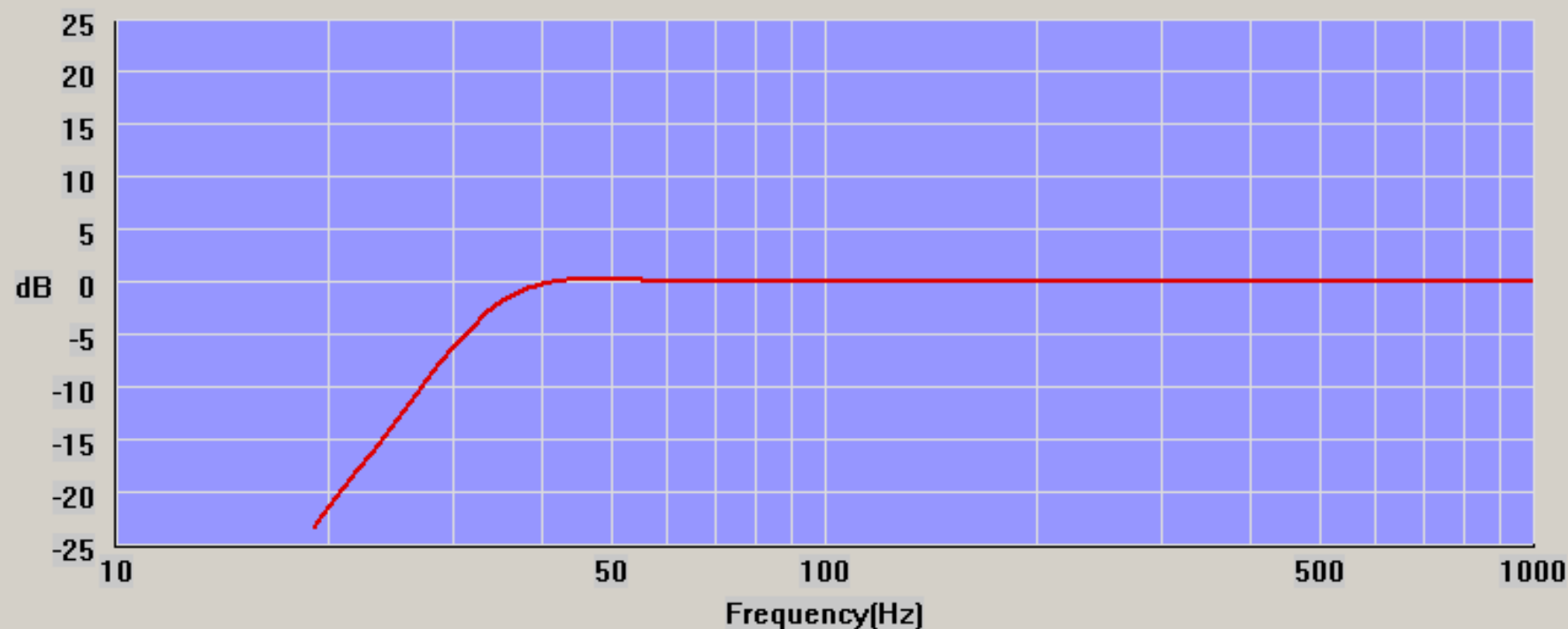
Vb: liters

Fb: Hz

F3: Hz

Lp: cm

Frequency Response: Output vs. Frequency



Speaker Parameters

Qts: Diameter: cm
 Qes: Xmax: mm Alignment:
 Fs: Hz Dp: cm ☐ SBB4
 Vas: liters # Ports: ☐ QB3
 Pmax: watts ☒ SC4

Calculate

www.ajdesigner.com

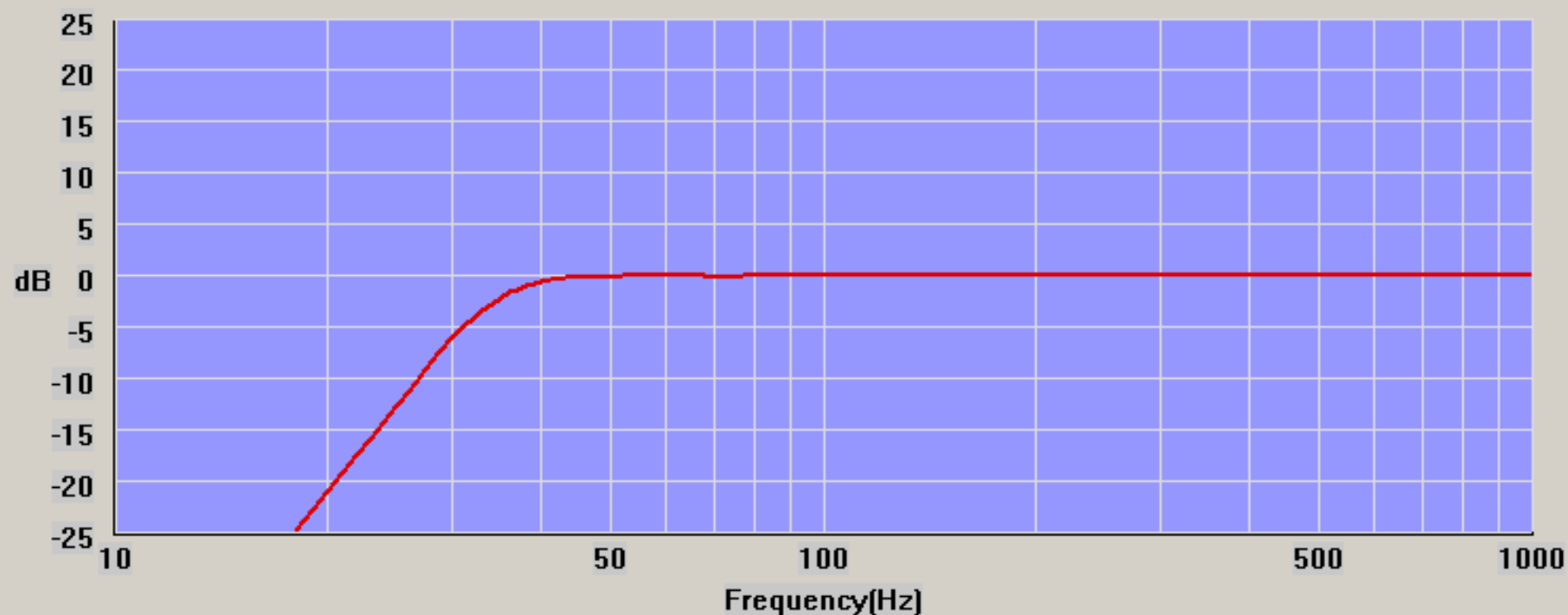
☒ Output Response

☐ Power Response

Box Results

Vb: liters
 Fb: Hz
 F3: Hz
 Lp: cm

Frequency Response: Output vs. Frequency



Box Calculator



Vb (liter):

Addl. V (liter):

Port Volume (liter):

Total Volume (liter):

Length (cm): ☐ Constrain

Width (cm): ☐ Constrain

Depth (cm): ☐ Constrain

Calculate

Cancel

